

Ch.5 Unit Circle Practice

NAME:

PER:

A. Define each function in terms of x and y (based on the unit circle with r = 1)

$$\sin \theta = \quad \cos \theta = \quad \tan \theta = \quad \csc \theta = \quad \sec \theta = \quad \cot \theta =$$

B. Principal Values: To find a unique solution for $\sin x$ and $\tan x$, refer only to Quadrant ___ or ___

To find a unique solution for $\cos x$, refer only to Quadrant ___ or ___

Refer to one of your unit circles resource pages from the past few days to answer the following questions:

Evaluate using exact answers.

No calculator!!

$$1. \sin \frac{5\pi}{3} =$$

$$2. \cos \frac{5\pi}{6} =$$

$$3. \tan \frac{2\pi}{4} =$$

$$4. \tan \left(-\frac{5\pi}{4}\right) =$$

$$5. \cos \frac{8\pi}{3} =$$

$$6. \cos \left(-\frac{5\pi}{6}\right) =$$

$$7. \tan \frac{7\pi}{4} =$$

$$8. \sin \frac{3\pi}{4} =$$

$$9. \cos \frac{11\pi}{6} =$$

$$10. \tan \frac{10\pi}{6} =$$

$$11. \sin \frac{5\pi}{2} =$$

$$12. \tan \frac{5\pi}{6} =$$

$$13. \sin \pi =$$

$$14. \sin \frac{5\pi}{4} =$$

$$15. \tan \frac{8\pi}{6} =$$

$$16. \sin \frac{19\pi}{6} =$$

$$17. \cos \frac{5\pi}{3} =$$

$$18. \tan \frac{5\pi}{4} =$$

$$19. \cos \frac{5\pi}{6} =$$

$$20. \tan \left(-\frac{4\pi}{3}\right) =$$

Hint: TWO general solutions each!!

$$21. \arctan(1) =$$

HINT: same as $\tan^{-1}(1)$
→ rewrite as $\tan \theta = 1$, then evaluate

$$22. \tan^{-1}(0) =$$

$$23. \sin^{-1} \left(\frac{-2\sqrt{3}}{4} \right) =$$

$$24. \arccos(0) =$$

$$25. \cos^{-1} \left(\frac{-\sqrt{2}}{2} \right) =$$

$$26. \arcsin \left(\frac{1}{2} \right) =$$

Hint: ONE solution each!!

Sine and Tangent have principal values in quadrants I and IV only.

$$27. \text{Arcsin}(0) =$$

$$28. \text{Arctan} \left(\frac{\sqrt{3}}{3} \right) =$$

$$29. \text{Arctan}(-1) =$$

$$30. \text{Arctan} \left(\frac{-4\sqrt{3}}{4} \right) =$$

Hint for #1-20: add or subtract a rotation of 2π if given angle is less than 0 or greater than 2π

Check answers A, B, and #1-30:

-1	$\frac{-1}{2}$	$\frac{-\sqrt{3}}{2}$	$\frac{\sqrt{3}}{2}$	$\frac{\pi}{6}$	$\frac{-\pi}{3} \text{ or } \frac{5\pi}{3}$	$\frac{-\pi}{4} \text{ or } \frac{7\pi}{4}$	$\frac{5\pi}{4}$
-1	$\frac{1}{2}$	$\frac{-\sqrt{3}}{2}$	$\frac{-\sqrt{3}}{2}$	$\frac{\pi}{6}$	$\frac{4\pi}{3}$	$\frac{\pi}{4}$	$\frac{\pi}{2}$
1	$\frac{1}{2}$	$\frac{-\sqrt{3}}{2}$	$\frac{-\sqrt{3}}{2}$	$\frac{5\pi}{6}$	$\frac{5\pi}{3}$	$\frac{3\pi}{4}$	$\frac{3\pi}{2}$
0	$\frac{-\sqrt{2}}{2}$	$\frac{-\sqrt{3}}{2}$	$-\sqrt{3}$	undefined	x	$\frac{5\pi}{4}$	
0	$\frac{2}{2}$	$\frac{2}{2}$	$-\sqrt{3}$		y		
0	$\frac{\sqrt{2}}{2}$	$\frac{-\sqrt{3}}{2}$	$\sqrt{3}$				
$-\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{-\sqrt{3}}{2}$	$\sqrt{3}$	$\frac{y}{x}$	$\frac{x}{y}$	$\frac{1}{x}$	$\frac{1}{y}$
							π
	I	II	I	IV			